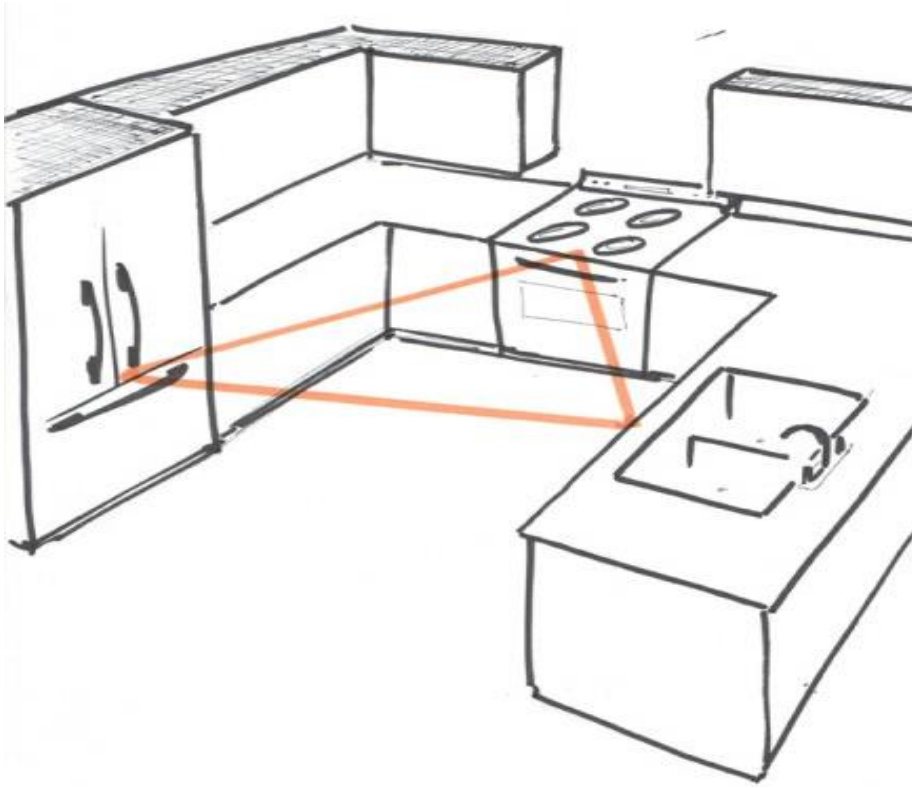


# Inequalities in One Triangle

## Lesson 5.5



## The Kitchen *Triangle*

For efficient movement in the kitchen home designers follow some simple rules in kitchen design.

## 5-5

Indirect Proof and Inequalities  
in One Triangle

## Theorems

## Angle-Side Relationships in Triangles

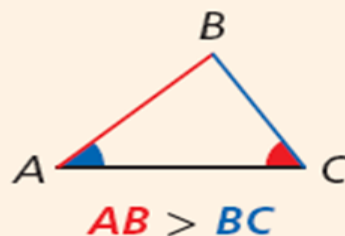
## THEOREM

## HYPOTHESIS

## CONCLUSION

**5-5-1** If two sides of a triangle are not congruent, then the larger angle is opposite the longer side.

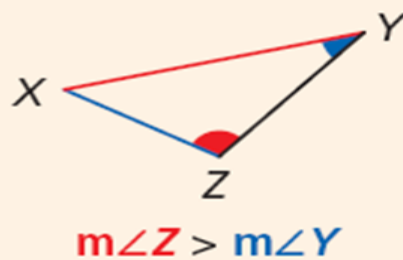
(In  $\triangle$ , larger  $\angle$  is opp. longer side.)



$$m\angle C > m\angle A$$

**5-5-2** If two angles of a triangle are not congruent, then the longer side is opposite the larger angle.

(In  $\triangle$ , longer side is opp. larger  $\angle$ .)



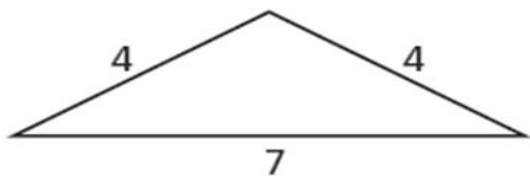
$$XY > XZ$$

## 5-5

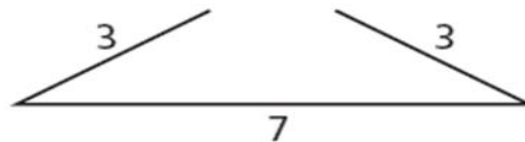
# Indirect Proof and Inequalities in One Triangle

CAN ANY THREE SEGMENTS MAKE A TRIANGLE?

Segments with lengths of 7, 4, and 4 can form a triangle.



Segments with lengths of 7, 3, and 3 cannot form a triangle.



# 5-5

# Indirect Proof and Inequalities in One Triangle

## Theorem 5-5-3

### Triangle Inequality Theorem

The sum of any two side lengths of a triangle is greater than the third side length.

$$AB + BC > AC$$

$$BC + AC > AB$$

$$AC + AB > BC$$

